Y11 to Y12 Mathematics Summer Independent Learning

June to August 2022

Please read the following instructions very carefully and ensure you label and collate all your work ready for checking in September.

For your first maths lesson please bring

- A large A4 folder with five subject dividers.
- These instructions with the tables filled in (print out/copy the tables onto A4 paper).
- Dated and titled work done on each of the topics listed in Task 1 & 3.
- The two practice initial tests (Task 2), fully marked and reviewed.
- A list of questions you need to ask prior to doing your initial test.

Task 1: Preparation for A level Maths

1. For each topic, work through video.
2. Complete worksheet **using the technique and layout** used in the video.
3. Make sure you title and date your work.
4. Mark and correct work.
5. Do improvement work as necessary.
6. Repeat for each topic.
7. Keep track by filling in the following table.
8. Collate your work for each topic together so it is easy to check in September. *(See point 3!)*

Topic	Video(s) *(Tick)*	Worksheet *(Tick)*	Details of Improvement Work Completed
B1 Indices			
B2 Surds			
B3 Quadratics			
B4 Simultaneous Equations			
B5 Inequalities			
E1 Triangle Geometry			

Task 2

1. Do Practice Initial Test 1 under exam conditions.
2. Mark and correct your test and identify any improvement work necessary.
3. Fill in the review sheet below.
4. Revisit relevant videos and worksheets.
5. Update review sheet with details of work completed.

Topic	Score	Improvement Work to Do	Tick
B1 Indices	11		
B2 Surds	10		
B3 Quadratics	49		
B4 Simultaneous Equations	11		
B5 Inequalities	11		
E1 Triangle Geometry	12		
Total	114		

6. Do Practice Initial Test 2 under exam conditions.
7. Mark and correct your test and identify any improvement work necessary.
8. Fill in the review sheet below.
9. Revisit relevant videos and worksheets.
10. Update review sheet with details of work completed.
11. Make a list of questions you need to ask prior to doing your initial test for real!

Topic	Score	Improvement Work to Do	Tick	Questions to ask…
B1 Indices	11			
B2 Surds	10			
B3 Quadratics	49			
B4 Simultaneous Equations	11			
B5 Inequalities	11			
E1 Triangle Geometry	12			
Total	114			

Video hyperlinks

B1 Indices

https://youtu.be/1lThXgU08S0

https://youtu.be/v5bn4HZrmQs

https://youtu.be/W0h4rHj88ys

B2 Surds

https://youtu.be/jHelde32YtI

B3 Quadratics

https://youtu.be/Pziws8ojnlk

https://youtu.be/sn_joGVj15w

https://youtu.be/kk7p6hjn7hQ

https://youtu.be/toIqbX_NXHo

B4 Simultaneous Equations

https://youtu.be/4SRtwS5unwE

B5 Inequalities

https://youtu.be/wDut-In_7Wg

E1 Triangle Geometry

https://youtu.be/uVl6TAb0vBg

Topic: B1 Indices

Exam Questions *(OCR/MEI C1 Questions)*

1. Jan 05 Q5

Find the value of the following.

(i) $\left(\frac{1}{3}\right)^{-2}$ [2]

(ii) $16^{\frac{3}{4}}$ [2]

2. June 05 Q6

Simplify the following.

(i) a^0 [1]

(ii) $a^6 \div a^{-2}$ [1]

(iii) $(9a^6b^2)^{-\frac{1}{2}}$ [3]

3. June 06 Q9

Simplify the following.

(i) $\frac{16^{\frac{1}{2}}}{81^{\frac{3}{4}}}$ [2]

(ii) $\frac{12(a^3b^2c)^4}{4a^2c^6}$ [3]

4. Jan 07 Q6

Find the value of each of the following, giving each answer as an integer or fraction as appropriate.

(i) $25^{\frac{3}{2}}$ [2]

(ii) $\left(\frac{7}{3}\right)^{-2}$ [2]

5. June 07 Q5

(i) Find a, given that $a^3 = 64x^{12}y^3$. [2]

(ii) Find the value of $\left(\frac{1}{2}\right)^{-5}$. [2]

Indices Exam Questions Solutions

1. Jan 05 Q5

(i) $\left(\frac{1}{3}\right)^{-2}$

$= \left(\frac{3}{1}\right)^{2}$

$= 9$

(ii) $16^{3/4}$

$= (16^{1/4})^{3}$

$= 2^{3}$

$= 8$

2. Jan 05 Q6

(i) $a^{0} = 1$ (ii) $a^{6} \div a^{-2} = a^{8}$

(iii) $(9a^{6}b^{2})^{-1/2} = \frac{1}{3}a^{-3}b^{-1}$

or $\frac{1}{3a^{3}b}$

3. June 06 Q9

(i) $\frac{16^{1/2}}{81^{3/4}}$

$= \frac{4}{(81^{1/4})^{3}}$

$= \frac{4}{3^{3}}$

$= \frac{4}{27}$

(ii) $\frac{12(a^{3}b^{2}c)^{4}}{4a^{2}c^{6}}$

$= \frac{12a^{12}b^{8}c^{4}}{4a^{2}c^{6}}$

$= 3a^{10}b^{8}c^{-2}$

or $\frac{3a^{10}b^{8}}{c^{2}}$

4. Jan 07 Q6

(i) $25^{3/2} = (25^{1/2})^{3}$

$= 5^{3}$

$= 125$

(ii) $\left(\frac{7}{3}\right)^{-2} = \left(\frac{3}{7}\right)^{2}$

$= \frac{9}{49}$

5. June 07 Q5

(i) $a^{3} = 64x^{12}y^{3}$

$a = (64x^{12}y^{3})^{1/3}$

$a = 4x^{4}y$

(ii) $\left(\frac{1}{2}\right)^{-5}$

$= \left(\frac{2}{1}\right)^{5}$

$= 32$

Topic: B2 Surds

Exam Questions *(AQA Questions)*

1. Jan 05 Q5

(a) Simplify $(\sqrt{12}+2)(\sqrt{12}-2)$. *(2 marks)*

(b) Express $\sqrt{12}$ in the form $m\sqrt{3}$, where m is an integer. *(1 mark)*

(c) Express $\dfrac{\sqrt{12}+2}{\sqrt{12}-2}$ in the form $a+b\sqrt{3}$, where a and b are integers. *(4 marks)*

2. June 05 Q5

Express each of the following in the form $m+n\sqrt{3}$, where m and n are integers:

(a) $(\sqrt{3}+1)^2$; *(2 marks)*

(b) $\dfrac{\sqrt{3}+1}{\sqrt{3}-1}$. *(3 marks)*

3. Jan 06 Q1

(a) Simplify $(\sqrt{5}+2)(\sqrt{5}-2)$. *(2 marks)*

(b) Express $\sqrt{8}+\sqrt{18}$ in the form $n\sqrt{2}$, where n is an integer. *(2 marks)*

4. June 06 Q4

(a) Express $(4\sqrt{5}-1)(\sqrt{5}+3)$ in the form $p+q\sqrt{5}$, where p and q are integers. *(3 marks)*

(b) Show that $\dfrac{\sqrt{75}-\sqrt{27}}{\sqrt{3}}$ is an integer and find its value. *(3 marks)*

5. Jan 07 Q3

(a) Express $\dfrac{\sqrt{5}+3}{\sqrt{5}-2}$ in the form $p\sqrt{5}+q$, where p and q are integers. *(4 marks)*

(b) (i) Express $\sqrt{45}$ in the form $n\sqrt{5}$, where n is an integer. *(1 mark)*

(ii) Solve the equation

$$x\sqrt{20} = 7\sqrt{5} - \sqrt{45}$$

giving your answer in its simplest form. *(3 marks)*

6. June 07 Q7

(a) Express $\dfrac{\sqrt{63}}{3}+\dfrac{14}{\sqrt{7}}$ in the form $n\sqrt{7}$, where n is an integer. *(3 marks)*

(b) Express $\dfrac{\sqrt{7}+1}{\sqrt{7}-2}$ in the form $p\sqrt{7}+q$, where p and q are integers. *(4 marks)*

Exam Questions Solutions - Surds

1. Jan 05 Q5

(a) $(\sqrt{12}+2)(\sqrt{12}-2)$ (M1)

$= 12 - 2\sqrt{12} + 2\sqrt{12} - 4$

$= 8$ (A1)

(b) $\sqrt{12} = \sqrt{4}\sqrt{3}$

$= 2\sqrt{3}$ (B1)

(c) $\dfrac{(\sqrt{12}+2)(\sqrt{12}+2)}{(\sqrt{12}-2)(\sqrt{12}+2)}$ (M1)

$= \dfrac{12+2\sqrt{12}+2\sqrt{12}+4}{8}$ (A1)

$= \dfrac{16+4\sqrt{12}}{8}$

$= \dfrac{16+8\sqrt{3}}{8}$ (A1)

$= 2+\sqrt{3}$ (A1)

2. June 05 Q5

(a) $(\sqrt{3}+1)^2$

$= (\sqrt{3}+1)(\sqrt{3}+1)$ (M1)

$= 3+\sqrt{3}+\sqrt{3}+1$

$= 4+2\sqrt{3}$ (A1)

(b) $\dfrac{(\sqrt{3}+1)(\sqrt{3}+1)}{(\sqrt{3}-1)(\sqrt{3}+1)}$ (M1)

$= \dfrac{4+2\sqrt{3}}{3+\sqrt{3}-\sqrt{3}-1}$ (A1)

$= \dfrac{4+2\sqrt{3}}{2}$

$= 2+\sqrt{3}$ (A1)

3. Jan 06 Q1

(a) $(\sqrt{5}+2)(\sqrt{5}-2)$

$= 5 - 2\sqrt{5} + 2\sqrt{5} - 4$ (M1)

$= 1$ (A1)

(b) $\sqrt{8} + \sqrt{18}$

$= \sqrt{4}\sqrt{2} + \sqrt{9}\sqrt{2}$ (M1)

$= 2\sqrt{2} + 3\sqrt{2}$

$= 5\sqrt{2}$ (A1)

4. June 06 Q4

(a) $(4\sqrt{5}-1)(\sqrt{5}+3)$

$= 20 + 12\sqrt{5} - \sqrt{5} - 3$ (M1)(A1)

$= 17 + 11\sqrt{5}$ (A1)

(b) $\dfrac{\sqrt{75}-\sqrt{27}}{\sqrt{3}}$

$= \dfrac{5\sqrt{3}-3\sqrt{3}}{\sqrt{3}}$ (M1)

$= \dfrac{2\sqrt{3}}{\sqrt{3}}$ (M1)

$= 2$ (A1)

5. Jan 07 Q3

(a) $\frac{(\sqrt{5}+3)(\sqrt{5}+2)}{(\sqrt{5}-2)(\sqrt{5}+2)}$ (m1)

$= \frac{5+2\sqrt{5}+3\sqrt{5}+6}{5-4}$ (A1) (A1)

$= 11 + 5\sqrt{5}$ (A1)

(b)(i) $\sqrt{45} = \sqrt{9}\sqrt{5}$ (B1)

$= 3\sqrt{5}$

(ii) $x\sqrt{20} = 7\sqrt{5} - \sqrt{45}$

$2x\sqrt{5} = 7\sqrt{5} - 3\sqrt{5}$ (m1)

$2x\sqrt{5} = 4\sqrt{5}$ (m1)

$2x = 4$

$x = 2$ (A1)

6. June 07 Q7

(a) $\frac{\sqrt{63}}{3} + \frac{14}{\sqrt{7}}$ (m1)

$= \frac{3\sqrt{7}}{3} + \frac{14}{\sqrt{7}} \cdot \frac{\sqrt{7}}{\sqrt{7}}$ (m1)

$= \frac{3\sqrt{7}}{3} + \frac{14\sqrt{7}}{7}$

$= \sqrt{7} + 2\sqrt{7}$

$= 3\sqrt{7}$ (A1)

(b) $\frac{(\sqrt{7}+1)(\sqrt{7}+2)}{(\sqrt{7}-2)(\sqrt{7}+2)}$ (m1)

$= \frac{7+2\sqrt{7}+\sqrt{7}+2}{7-4}$ (A1) (A1)

$= \frac{9+3\sqrt{7}}{3}$

$= 3 + \sqrt{7}$ (A1)

Topic: B3 Quadratics

Exam Questions *(AQA C1 Questions)*

1. Jan 2011 Q7

(a) (i) Express $4 - 10x - x^2$ in the form $p - (x + q)^2$. *(2 marks)*

(ii) Hence write down the equation of the line of symmetry of the curve with equation $y = 4 - 10x - x^2$. *(1 mark)*

2. June 11 Q4

(a) Express $x^2 + 5x + 7$ in the form $(x + p)^2 + q$, where p and q are rational numbers. *(3 marks)*

(b) A curve has equation $y = x^2 + 5x + 7$.

(i) Find the coordinates of the vertex of the curve. *(2 marks)*

(ii) State the equation of the line of symmetry of the curve. *(1 mark)*

(iii) Sketch the curve, stating the value of the intercept on the y-axis. *(3 marks)*

(c) Describe the geometrical transformation that maps the graph of $y = x^2$ onto the graph of $y = x^2 + 5x + 7$. *(3 marks)*

3. Jan 12 Q2

(a) Factorise $x^2 - 4x - 12$. *(1 mark)*

(b) Sketch the graph with equation $y = x^2 - 4x - 12$, stating the values where the curve crosses the coordinate axes. *(4 marks)*

(c) (i) Express $x^2 - 4x - 12$ in the form $(x - p)^2 - q$, where p and q are positive integers. *(2 marks)*

(ii) Hence find the minimum value of $x^2 - 4x - 12$. *(1 mark)*

(d) The curve with equation $y = x^2 - 4x - 12$ is translated by the vector $\begin{bmatrix} -3 \\ 2 \end{bmatrix}$.
Find an equation of the new curve. You need not simplify your answer. *(2 marks)*

4. June 12 Q5

(a) (i) Express $x^2 - 3x + 5$ in the form $(x - p)^2 + q$. *(2 marks)*

(ii) Hence write down the equation of the line of symmetry of the curve with equation $y = x^2 - 3x + 5$. *(1 mark)*

5. **Jan 13 Q4**

(a) (i) Express $x^2 - 6x + 11$ in the form $(x - p)^2 + q$. *(2 marks)*

(ii) **Use the result from part (a)(i)** to show that the equation $x^2 - 6x + 11 = 0$ has no real solutions. *(2 marks)*

(b) A curve has equation $y = x^2 - 6x + 11$.

(i) Find the coordinates of the vertex of the curve. *(2 marks)*

(ii) Sketch the curve, indicating the value of y where the curve crosses the y-axis. *(3 marks)*

(iii) Describe the geometrical transformation that maps the curve with equation $y = x^2 - 6x + 11$ onto the curve with equation $y = x^2$. *(3 marks)*

6. **June 13 Q5**

(a) (i) Express $2x^2 + 6x + 5$ in the form $2(x + p)^2 + q$, where p and q are rational numbers. *(2 marks)*

(ii) Hence write down the minimum value of $2x^2 + 6x + 5$. *(1 mark)*

Quadratics Exam Questions Solutions

1. Jan 2011 Q7

(a)(i) $4 - 10x - x^2$

$\equiv -(x^2 + 10x - 4)$

$\equiv -((x+5)^2 - 25 - 4)$ (M1)

$\equiv -((x+5)^2 - 29)$

$\equiv 29 - (x+5)^2$ (A1)

(ii) line of symmetry $x = -5$ (B1FT)

2. June 11 Q4

(a) $x^2 + 5x + 7 \equiv$

$\equiv (x + 5/2)^2 - \frac{25}{4} + \frac{28}{4}$ (B1)(M1)

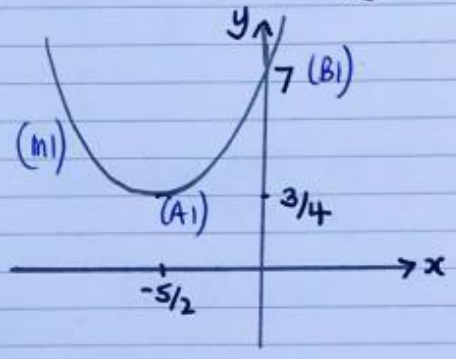
$\equiv (x + \frac{5}{2})^2 + \frac{3}{4}$ (A1)

(b) (i) when $x = -\frac{5}{2}$ $y = \frac{3}{4}$ (M1)

$\therefore$ vertex at $(-5/2, 3/4)$ (A1)

(ii) line of symmetry $x = -\frac{5}{2}$ (B1FT)

(iii)



(c) Translation $\begin{pmatrix} -5/2 \\ 3/4 \end{pmatrix}$ (M1)(A1)

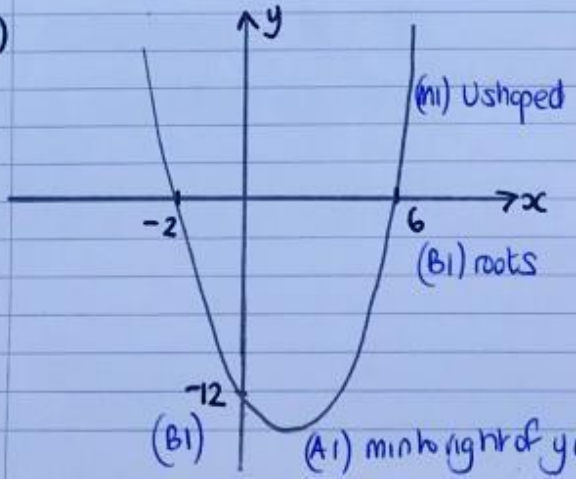
(E1)

3. Jan 12 Q2

(a) $x^2 - 4x - 12$

$\equiv (x-6)(x+2)$ (B1)

(b)



(c)(i) $x^2 - 4x - 12$

$\equiv (x-2)^2 - 4 - 12$ (M1)

$\equiv (x-2)^2 - 16$ (A1)

(ii) min value is -16 (B1FT)

(d) $y = (x+3)^2 - 4(x+3) - 12 + 2$ (M1)

$y = (x+3)^2 - 4(x+3) - 10$

or any equivalent form (A1)

ie $y = (x+1)^2 - 14$

4. June 12 Q5

(a)(i) $x^2 - 3x + 5$

$\equiv (x - 3/2)^2 - \frac{9}{4} + \frac{20}{4}$ (M1)

$\equiv (x - 3/2)^2 + \frac{11}{4}$ (A1)

(ii) line of symmetry is $x = 3/2$ (B1FT)

5. Jan 13 Q4

(a)(i) $x^2 - 6x + 11$

$\equiv (x-3)^2 - 9 + 11$ (M1)

$\equiv (x-3)^2 + 2$ (A1)

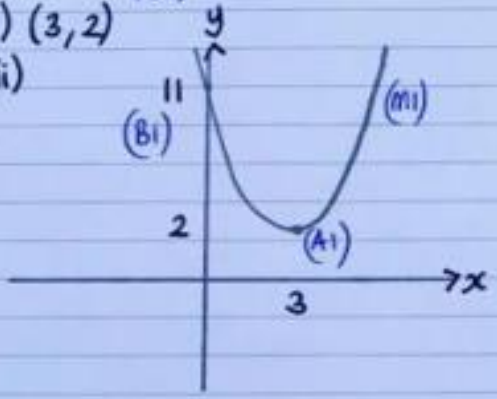
(ii) $(x-3)^2 + 2 = 0$

$(x-3)^2 = -2$ (M1)

can't take square root of negative number and get real solutions ∴ no real solutions (A1)

(b)(i) (3, 2) (M1)(A1)

(b)(ii)



(iii) Translation $\begin{pmatrix} -3 \\ -2 \end{pmatrix}$ (M1) (A1)

(E1)

Gone backwards !

6 June 13 Q5

(a)(i) $2x^2 + 6x + 5$

$\equiv 2[x^2 + 3x] + 5$

$\equiv 2[(x+3/2)^2 - 9/4] + 5$ (M1)

$\equiv 2(x+3/2)^2 - 9/2 + 10/2$

$\equiv 2(x+3/2)^2 + 1/2$ (A1)

or $2x^2 + 6x + 5$

$\equiv 2[x^2 + 3x + 5/2]$

$\equiv 2[(x+3/2)^2 - 9/4 + 10/4]$

$\equiv 2[(x+3/2)^2 + 1/4]$

$\equiv 2(x+3/2)^2 + 1/2$

(ii) Min value is $y = 1/2$ (B1FT)

Topic B4 Simultaneous equations

Exam Questions *(AQA C1 Questions)*

1

Solve the simultaneous equations

$$y - 3x + 2 = 0$$

$$y^2 - x - 6x^2 = 0$$

(Total 7 marks)

2

The curve C has equation $y = x^2 - 4$ and the straight line l has equation $y + 3x = 0$.

(a) In the space below, sketch C and l on the same axes.

(3)

(b) Write down the coordinates of the points at which C meets the coordinate axes.

(2)

(c) Using algebra, find the coordinates of the points at which l intersects C.

(4)

(Total 9 marks)

3 **Jan 011 Q7**

(b) The curve C has equation $y = 4 - 10x - x^2$ and the line L has equation $y = k(4x - 13)$, where k is a constant.

(i) Show that the x-coordinates of any points of intersection of the curve C with the line L satisfy the equation

$$x^2 + 2(2k + 5)x - (13k + 4) = 0 \qquad \textit{(1 mark)}$$

4. **Jan 13 Q8**

A curve has equation $y = 2x^2 - x - 1$ and a line has equation $y = k(2x - 3)$, where k is a constant.

(a) Show that the x-coordinate of any point of intersection of the curve and the line satisfies the equation

$$2x^2 - (2k + 1)x + 3k - 1 = 0 \qquad \textit{(1 mark)}$$

Simultaneous Equations Exam Questions

1) $y = 3x - 2$

$(3x-2)^2 - x - 6x^2 = 0$

$9x^2 - 12x + 4 - x - 6x^2 = 0$

$3x^2 - 13x + 4 = 0$

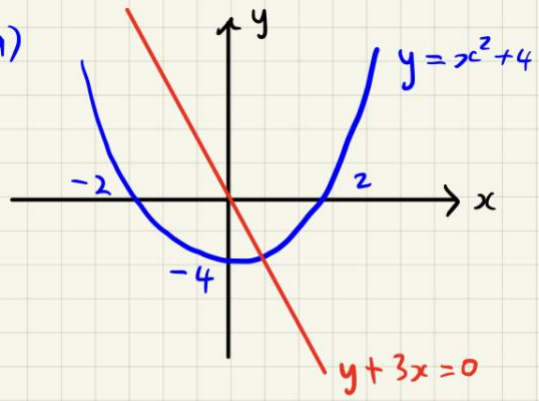
$(3x - 1)(x - 4) = 0$

$x = 1/3$ or $x = 4$

$y = -1$ $y = 10$

2)

a)



b) $(2,0)$, $(-2,0)$

c) $y = -3x$

$-3x = x^2 - 4$

$x^2 + 3x - 4 = 0$

$(x - 1)(x + 4) = 0$

$x = 1$ OR $x = -4$

$y = -3$ $y = 12$

intersections are $(1, -3)$, $(-4, 12)$

Jan 11 Q7

$y = 4 - 10x - x^2 \qquad y = k(4x - 13)$

$k(4x - 13) = 4 - 10x - x^2$

$x^2 + 10x + 4kx - 13k - 4 = 0$

$x^2 + 2(2k + 5)x - (13k + 4) = 0$

Jan 13 Q8

$y = 2x^2 - x - 1 \qquad y = k(2x - 3)$

$2x^2 - x - 1 = k(2x - 3)$

$2x^2 - x - 1 = 2kx - 3k$

$2x^2 - 2kx - x + 3k - 1 = 0$

$2x^2 - (2k + 1)x + 3k - 1 = 0$

Topic: B5 Inequalities

Exam Questions *(AQA C1 Questions)*

1.	**Jan 11 Q7** **(iii)** Solve the inequality $4k^2 + 33k + 29 > 0$. *(4 marks)*
2.	**June 11 Q7** Solve each of the following inequalities: **(a)** $2(4 - 3x) > 5 - 4(x + 2)$; *(2 marks)* **(b)** $2x^2 + 5x \geqslant 12$. *(4 marks)*
3.	**Jan 12 Q6** A rectangular garden is to have width x metres and length $(x + 4)$ metres. **(a)** The perimeter of the garden needs to be greater than 30 metres. Show that $2x > 11$. *(1 mark)* **(b)** The area of the garden needs to be less than 96 square metres. Show that $x^2 + 4x - 96 < 0$. *(1 mark)* **(c)** Solve the inequality $x^2 + 4x - 96 < 0$. *(4 marks)* **(d)** Hence determine the possible values of the width of the garden. *(1 mark)*
4.	**June 12 Q7a** **(ii)** Solve the inequality $3x^2 - 10x + 8 < 0$. *(4 marks)*

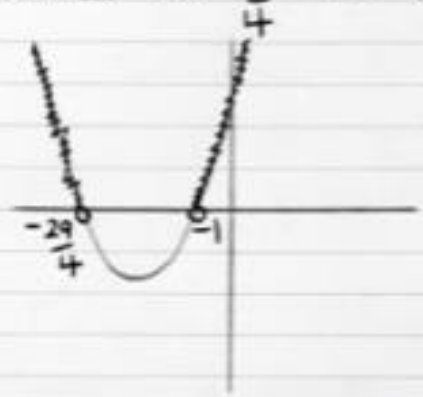
Inequalities Exam Questions Solutions

1. Jan 11 Q7 (ii)

$4R^2 + 33R + 29 > 0$

$(4R + 29)(R+1) > 0$ (m1)

cvs at $R = -\frac{29}{4}$ $R = -1$ (A1)



(m1)

$R < -\frac{29}{4}$ or $R > -1$ (A1)

4

2. June 11 Q7

(a) $2(4-3x) > 5 - 4(x+2)$

$8 - 6x > 5 - 4x - 8$ (m1)

$-2x > -11$

$2x < 11$ (x-1 reverse inequality sign)

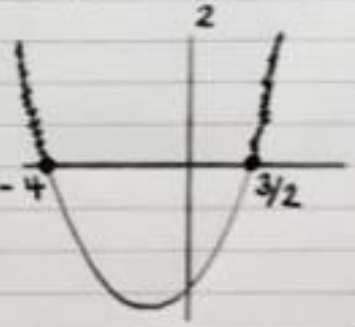
$x < \frac{11}{2}$ (A1)

(b) $2x^2 + 5x \geq 12$

$2x^2 + 5x - 12 \geq 0$

$(2x-3)(x+4) \geq 0$ (m1)

cvs at $x = \frac{3}{2}$ $x = -4$ (A1)

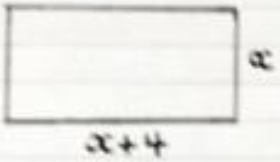


(m1)

$x \leq -4$ or $x \geq 3/2$ (A1)

6

3 Jan 12 Q6



(a) $x + x + x + 4 + x + 4 > 30$

$4x + 8 > 30$

$4x > 22$

$2x > 11$ (B1)

$(x > 1\frac{1}{2})$

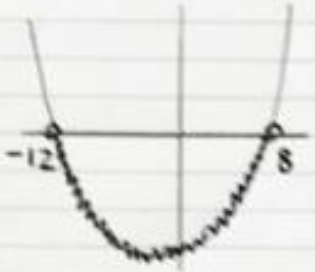
(b) $x(x+4) < 96$

$x^2 + 4x < 96$

$x^2 + 4x - 96 < 0$ (B1)

$(x+12)(x-8) < 0$ (M1)

cvs $x = -12$ $x = 8$ (A1)



(M1)

$-12 < x < 8$ (A1)

(c) $\frac{11}{2} < x < 8$ (B1)

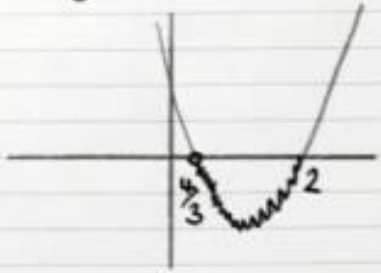
4

4. June 12 Q7(a)

$3x^2 - 10x + 8 < 0$

$(3x-4)(x-2) < 0$ (M1)

cvs $x = \frac{4}{3}$ $x = 2$ (A1)



(M1)

4

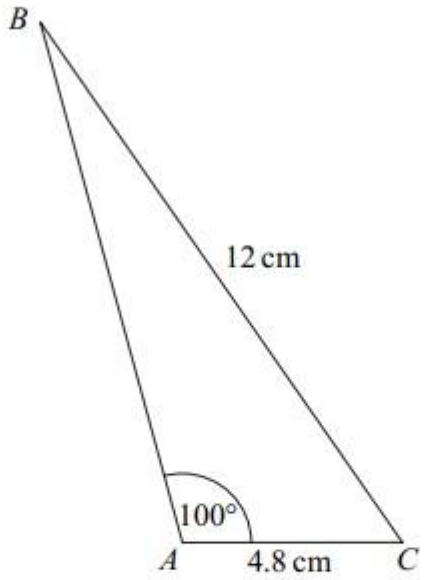
$\frac{4}{3} < x < 2$ (A1)

Topic E1 Triangle Geometry

Exam Questions *(AQA C2 Questions)*

1. June 2006 Q2

The diagram shows a triangle ABC.



The lengths of AC and BC are 4.8 cm and 12 cm respectively.

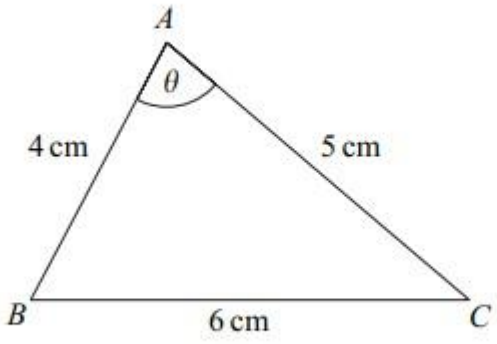
The size of the angle BAC is $100°$.

(a) Show that angle $ABC = 23.2°$, correct to the nearest $0.1°$. *(3 marks)*

(b) Calculate the area of triangle ABC, giving your answer in cm^2 to three significant figures. *(3 marks)*

2. Jan 2007 Q4 (adapted)

The triangle ABC, shown in the diagram, is such that $BC = 6$ cm, $AC = 5$ cm and $AB = 4$ cm. The angle BAC is θ.

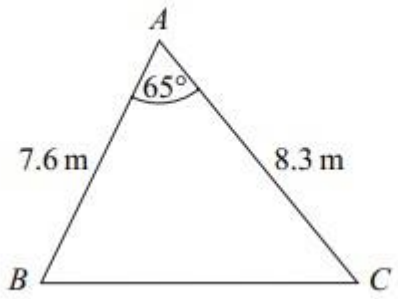


(a) Use the cosine rule to show that $\cos\theta = \frac{1}{8}$. *(3 marks)*

(c) Hence find the area of the triangle ABC. *(2 marks)*

3. **June 2008 Q4**

The diagram shows a triangle ABC.



The size of angle BAC is 65°, and the lengths of AB and AC are 7.6 m and 8.3 m respectively.

(a) Show that the length of BC is 8.56 m, correct to three significant figures. *(3 marks)*

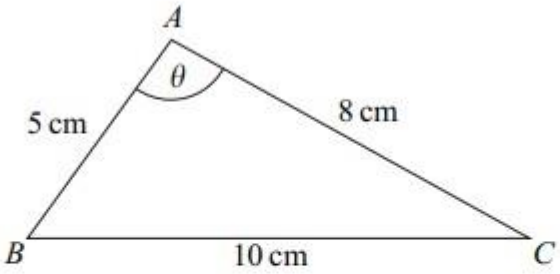
(b) Calculate the area of triangle ABC, giving your answer in m^2 to three significant figures. *(2 marks)*

(c) The perpendicular from A to BC meets BC at the point D.

Calculate the length of AD, giving your answer to the nearest 0.1 m. *(3 marks)*

4. **Jan 2011 Q3**

The triangle ABC, shown in the diagram, is such that $AB = 5$ cm, $AC = 8$ cm, $BC = 10$ cm and angle $BAC = \theta$.



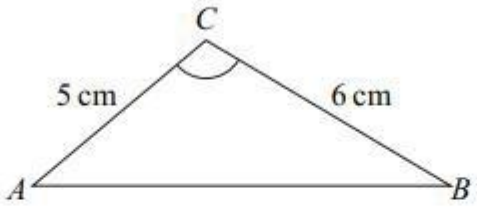
(a) Show that $\theta = 97.9°$, correct to the nearest 0.1°. *(3 marks)*

(b) (i) Calculate the area of triangle ABC, giving your answer, in cm^2, to three significant figures. *(2 marks)*

(ii) The line through A, perpendicular to BC, meets BC at the point D. Calculate the length of AD, giving your answer, in cm, to three significant figures. *(3 marks)*

5. **Jan 2013 Q3**

The diagram shows a triangle ABC.



The lengths of AC and BC are 5 cm and 6 cm respectively.

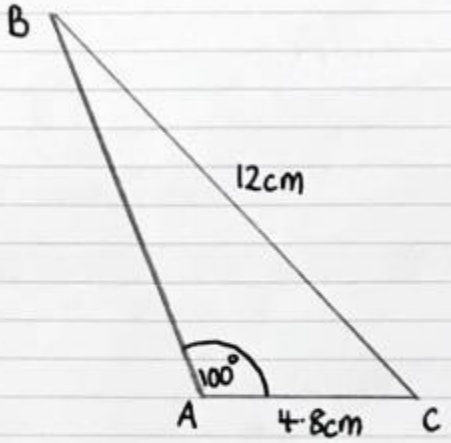
The area of triangle ABC is 12.5 cm^2, and angle ACB is **obtuse**.

(a) Find the size of angle ACB, giving your answer to the nearest 0.1°. *(3 marks)*

(b) Find the length of AB, giving your answer to two significant figures. *(3 marks)*

Triangle Geometry Exam Questions

1. June 2006 Q2



(a) $\frac{\sin A\hat{B}C}{4.8} = \frac{\sin 100}{12}$ (M1)

$\sin A\hat{B}C = 0.4\sin 100$ (M1)

$A\hat{B}C = \sin^{-1}(0.4\sin 100)$

$A\hat{B}C = 23.19882755$

$A\hat{B}C = 23.2$ correct to nearest 0.1° (A1)

(b) angle $A\hat{C}B = 180 - 100 - 23.2$

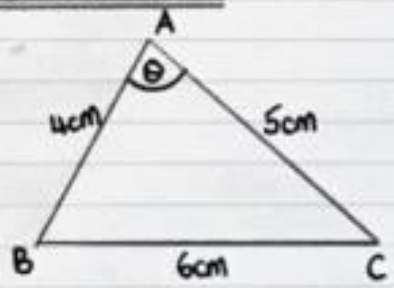
$= 56.8°$ (M1)

area of $\Delta = \frac{1}{2} \times 4.8 \times 12 \times \sin 56.8$ (M1)

$= 24.1\ cm^2$ to 3.s.f. (A1)

6

2. Jan 2007 Q4



(a) Using cosine rule (M1)

$6^2 = 4^2 + 5^2 - 2(4)(5)\cos\theta$

$36 = 41 - 40\cos\theta$

$40\cos\theta = 5$ (M1)

$\cos\theta = \frac{5}{40}$

$\cos\theta = \frac{1}{8}$ (A1)

(c) $\theta = \cos^{-1}\left(\frac{1}{8}\right)$

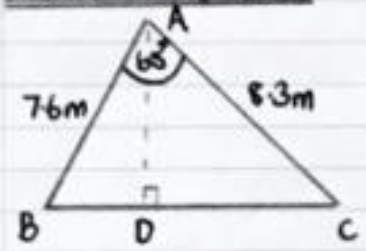
$\theta = 82.8°$ (M1)

$A = \frac{1}{2} \times 4 \times 5 \times \sin 82.8°$

Area = $9.92 cm^2$ to 3.s.f. (A1)

5

3. June 2008 Q4



(a) Using cosine rule

$BC^2 = 7.6^2 + 8.3^2 - 2(7.6)(8.3)\cos 65°$ (M1)

$BC^2 = 73.33248...$ (M1)

$BC = 8.5634...$

BC = 8.56m to 3.s.f. (A1)

(b) $A = \frac{1}{2} \times 7.6 \times 8.3 \sin 65$ (M1)

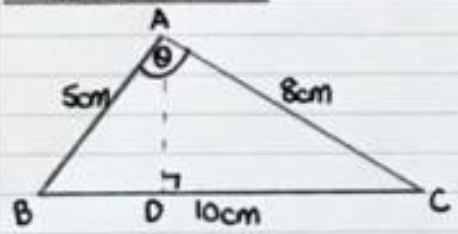
$= 28.6m^2$ to 3.s.f. (A1)

(c) $28.6 = \frac{1}{2} \times 8.56 \times AD$ (M1) (M1)

AD = 6.7m to nearest 0.1m (A1)

8

4. Jan 2011 Q3



(a) Using cosine rule

$10^2 = 5^2 + 8^2 - 2(5)(8)\cos\theta$ (M1)

$100 = 89 - 80\cos\theta$ (M1)

$80\cos\theta = -11$

$\cos\theta = \frac{-11}{80}$

$\theta = 97.9032...$

$\theta = 97.9°$ to nearest $0.1°$ (A1)

(b) (i) Area $= \frac{1}{2} \times 5 \times 8 \times \sin 97.9°$ (M1)

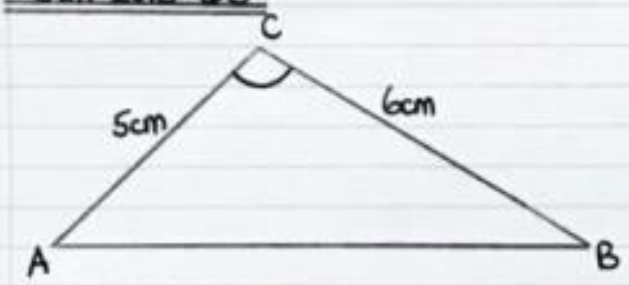
$= 19.8\text{cm}^2$ to 3.s.f. (A1)

(ii) $19.8 = \frac{1}{2} \times 10 \times AD$ (M1)(M1)

$AD = 3.96$ cm to 3.s.f. (A1)

/8

5. Jan 2013 Q3



(a) $12.5 = \frac{1}{2} \times 5 \times 6 \times \sin C$ (M1)

$\frac{12.5}{15} = \sin C$ (A1)

$C = 56.4°$

but $A\hat{C}B$ is obtuse

$\therefore A\hat{C}B = 180 - 56.4$

$= 123.6°$ (A1)

(b) Using cosine rule

$AB^2 = 5^2 + 6^2 - 2(5)(6)\cos 123.6°$ (M1)(M1)

$AB^2 = 94.203...$

$AB = 9.7$ cm to 2.s.f. (A1)

/6

TASK 2

Year 12 Initial Test for Mathematics

Write out the solutions to each of the following questions.
*Show full working, **without** the use of a calculator.*

Practice 1 (No Calculator)

B1 Indices

1.	Evaluate $\left(\frac{8}{125}\right)^{-2/3}$	**2.**	Express in the form x^k $\frac{\sqrt{x} \times \sqrt[3]{x}}{x^2}$	**3.**	Solve $9^{x-2} = 27$	**4.**	Solve $16^x = 4^{1-x}$

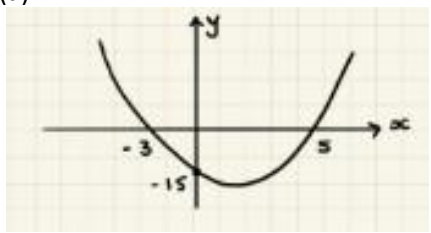
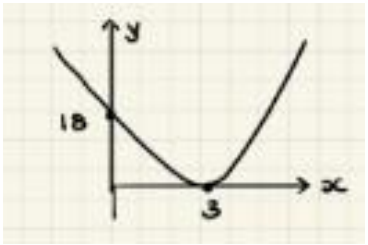
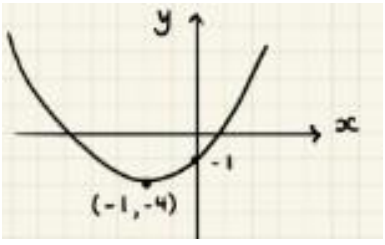
B2 Surds

1.	Simplify $\sqrt{72}$	**2.**	Expand and simplify $(2\sqrt{7} - 5\sqrt{3})(3\sqrt{7} + 4\sqrt{3})$	**3.**	Rationalise the denominator $\frac{11}{2\sqrt{5}}$	**4.**	Rationalise the denominator $\frac{8 - 3\sqrt{5}}{2 + \sqrt{5}}$

B3 Quadratics

1. Solve the following quadratic equations by factorising and use your solutions to sketch the related quadratic graph, labelling all intersections with the coordinate axis.		
(a) (i) $x^2 + 3x - 28 = 0$	(b) (i) $x^2 - 6x + 9 = 0$	(c) (i) $2x^2 - 21x + 27 = 0$
(a) (ii) Sketch $y = x^2 + 3x - 28$	(b) (ii) Sketch $y = x^2 - 6x + 9$	(c) (ii) Sketch $y = 2x^2 - 21x + 27$

2. Solve the following quadratic equations by completing the square and use your solutions to sketch the related quadratic graph, labelling all intersections with the coordinate axis and turning point.		
(a) (i) $x^2 + 4x - 7 = 0$	(b) (i) $11 + 8x - x^2 = 0$	(c) (i) $3x^2 - 12x + 2 = 0$
(ii) Write $y = x^2 + 4x - 7$ in the form $y = a(x + b)^2 + c$	(ii) Write $y = 11 + 8x - x^2$in the form $y = a(x + b)^2 + c$	(ii) Write $y = 3x^2 - 12x + 2$ in the form $y = a(x + b)^2 + c$
(iii) Sketch $y = x^2 + 4x - 7$	(iii) Sketch $y = 11 + 8x - x^2$	(iii) Sketch $y = 3x^2 - 12x + 2$

3. Evaluate the equation of the following quadratics, giving your answer in the form $y = ax^2 + bx + c$		
(a) 	(b) 	(c) 

B4 Simultaneous Equations

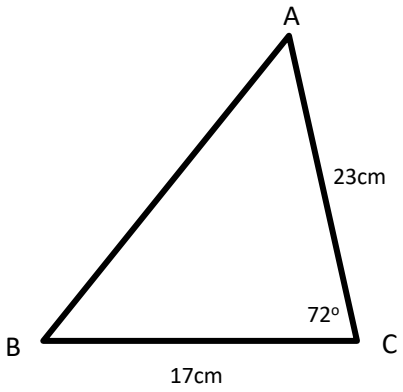
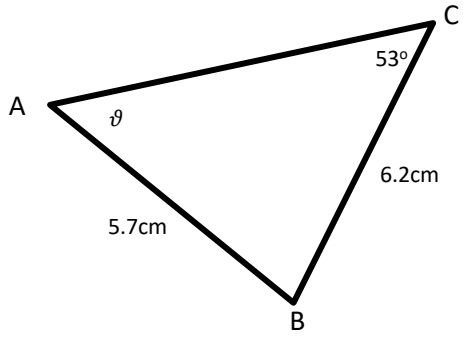
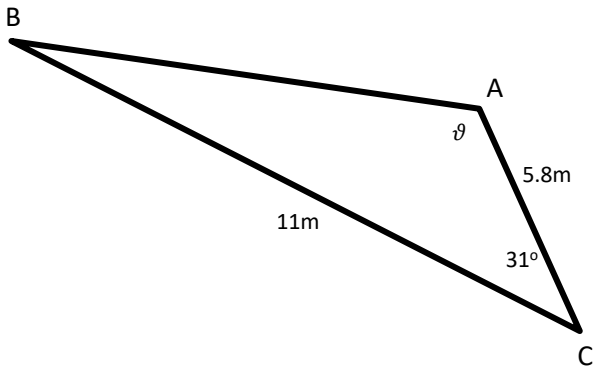
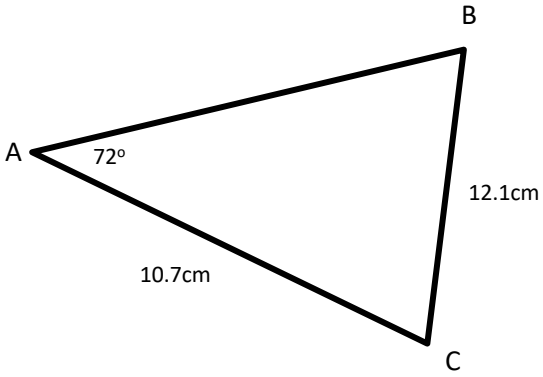
1.	Solve $3x + 3y = -4$ $5x - 2y = 5$	**2.**	Solve $y = x - 6$ $\frac{1}{2}x - y = 4$	**3.**	Solve $3x^2 - x - y^2 = 0$ $x + y = 1$

B5 Inequalities

Find the set of values for which…

1.	$3(1 - 2t) \leq t - 4$	**2.**	$2x^2 - 9x + 4 \leq 0$	**3.**	$2y + 3 < 3y(y - 2)$

E1 Triangle Geometry (Calculator)

1.	Calculate the length AB 	**2.**	Calculate the angle ϑ 
3.	Calculate the length AB and the obtuse angle ϑ 	**4.**	Calculate the area of the triangle ABC 

Practice 1

B1 Indices

1. $\left(\frac{8}{125}\right)^{-2/3}$

$= \left(\frac{125}{8}\right)^{2/3}$

$= \left(\frac{5}{2}\right)^{2}$ M1

$= \frac{25}{4}$ A1

2. $\frac{\sqrt{x} \times \sqrt[3]{x}}{x^2}$

$= \frac{x^{1/2} \times x^{1/3}}{x^2}$ M1

$= \frac{x^{5/6}}{x^2}$ A1

$= x^{-7/6}$ A1

3. $9^{x-2} = 27$

$(3^2)^{x-2} = 3^3$ M1

$3^{2x-4} = 3^3$

$2x - 4 = 3$ M1

$2x = 7$

$x = 7/2$ A1

4. $16^{x} = 4^{1-x}$

$(4^2)^{x} = 4^{1-x}$ M1

$4^{2x} = 4^{1-x}$ [1]

$2x = 1 - x$ M1

$3x = 1 \Rightarrow x = 1/3$ A1

B2 Surds

1. $\sqrt{72}$

$= \sqrt{36 \times 2}$

$= 6\sqrt{2}$ A1

2. $(2\sqrt{7} - 5\sqrt{3})(3\sqrt{7} + 4\sqrt{3})$

$42 + 8\sqrt{21} - 15\sqrt{21} - 60$ m1 A1

$-7\sqrt{21} - 18$ A1

3. $\frac{11}{2\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}}$ M1

$= \frac{11\sqrt{5}}{10}$ A1

4. $\frac{8 - 3\sqrt{5}}{2 + \sqrt{5}} \quad \frac{(2 - \sqrt{5})}{(2 - \sqrt{5})}$ M1

$= \frac{16 - 8\sqrt{5} - 6\sqrt{5} + 15}{4 - 5}$ A1 A1

$= \frac{31 - 14\sqrt{5}}{-1} = 14\sqrt{5} - 31$ A1

[10]

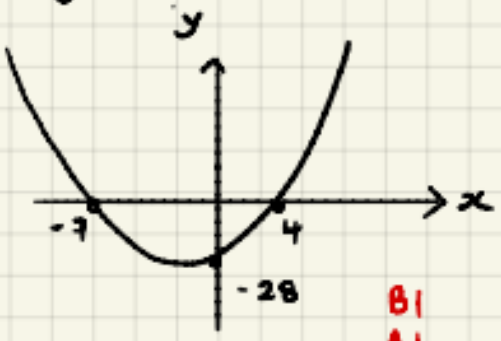
B3 Quadratics

1. (a) (i) $x^2 + 3x - 28 = 0$

$(x+7)(x-4) = 0$ M1

$x = -7$ or $x = 4$ A1

(ii) $y = x^2 + 3x - 28$



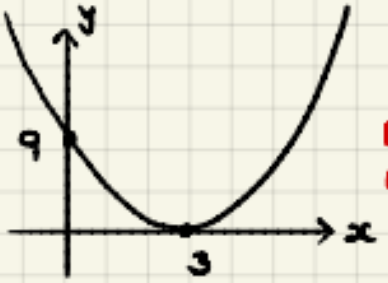
B1
A1
A1

(b) (i) $x^2 - 6x + 9 = 0$

$(x-3)^2 = 0$ M1

A1 $x = 3$ (repeated)

(ii) $y = x^2 - 6x + 9$



B1
A1
A1

(c) (i) $2x^2 - 21x + 27 = 0$

$(2x-3)(x-9) = 0$ M1

$x = 3/2$ $x = 9$ A1

(ii) $y = 2x^2 - 21x + 27$

B1
A1
A1

15

B1 shape, location related to axes

A1 intersections x-axis

A1 intersections y-axis

2. (a) (i) $x^2 + 4x - 7 = 0$

$(x+2)^2 - 4 - 7 = 0$ M1

$(x+2)^2 = 11$

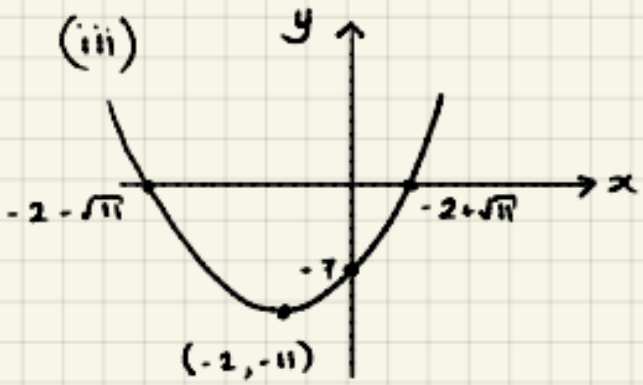
$x + 2 = \pm\sqrt{11}$

$x = -2 \pm \sqrt{11}$ A1

(ii) $y = x^2 + 4x - 7$

$y = (x+2)^2 - 11$ B1

(iii)



Graphs
- B1 Shape
- A1 Vertex
- A1 intersections x-axis
- A1 intersections y-axis

(b) (i) $11 + 8x - x^2 = 0$

$-(x^2 - 8x - 11) = 0$ M1

$-[(x-4)^2 - 16 - 11] = 0$ M1

$-(x-4)^2 + 27 = 0$

$(x-4)^2 = 27$

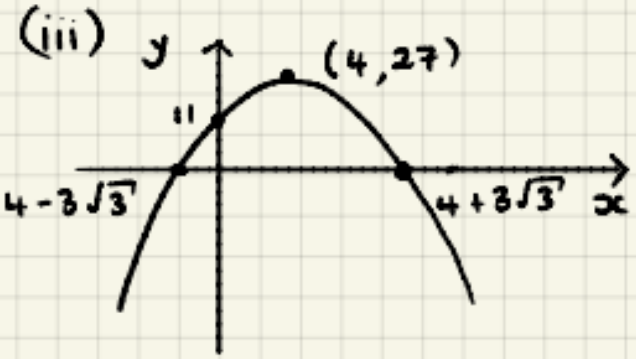
$x - 4 = \pm 3\sqrt{3}$

$x = 4 \pm 3\sqrt{3}$ A1

(ii) $y = 11 + 8x - x^2$

$y = 27 - (x-4)^2$ B1

(iii)



(c) (i) $3x^2 - 12x + 2 = 0$

$3\left[x^2 - 4x + \frac{2}{3}\right] = 0$ M1

$3\left[(x-2)^2 - 4 + \frac{2}{3}\right] = 0$ M1

$3\left[(x-2)^2 - \frac{10}{3}\right] = 0$

$3(x-2)^2 - 10 = 0$

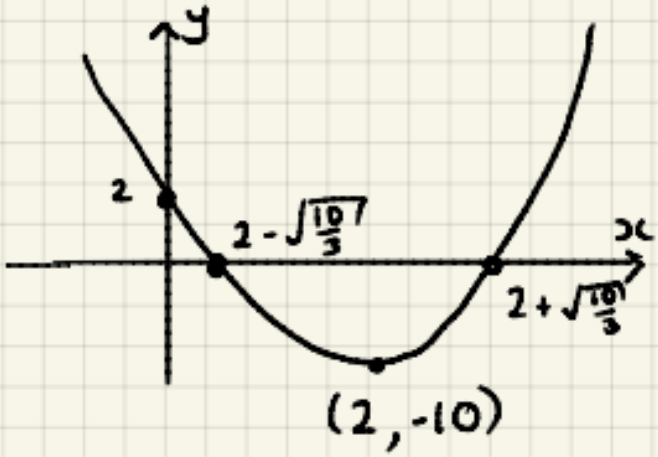
$(x-2)^2 = \frac{10}{3}$

$x - 2 = \pm\sqrt{\frac{10}{3}}$

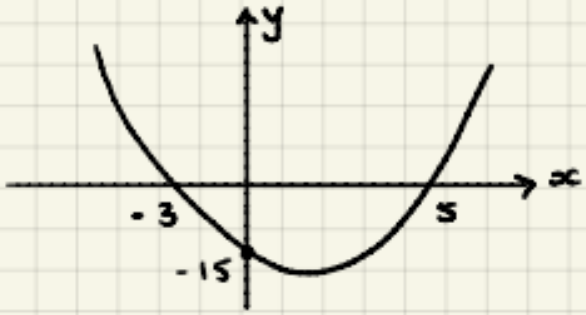
$x = 2 \pm \sqrt{\frac{10}{3}}$ A1

(ii) $y = 3x^2 - 12x + 2$

$y = 3(x-2)^2 - 10$ B1



3. (a)



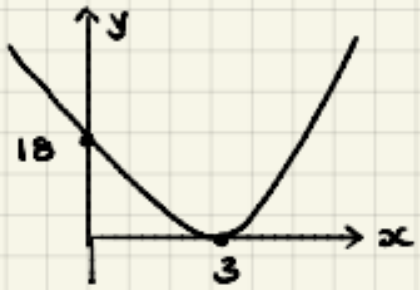
$y = k(x+3)(x-5)$ M1

$-15 = k(3)(-5) \Rightarrow k = 1$ A1

$y = (x+3)(x-5)$

$y = x^2 - 2x - 15$ A1

(b)



$y = k(x-3)^2$ M1

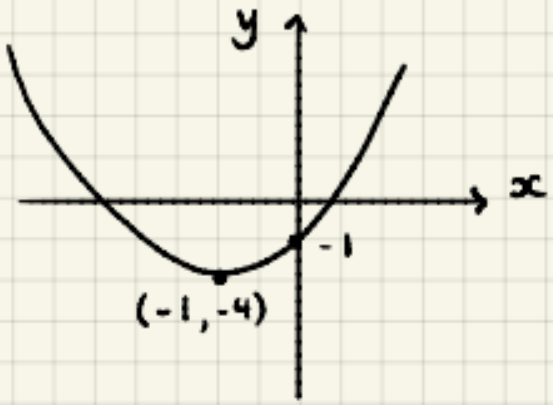
$18 = k(-3)^2 \Rightarrow k = 2$ A1

$y = 2(x-3)^2$

$y = 2(x^2 - 6x + 9)$

$y = 2x^2 - 12x + 18$ A1

(c)



$y = k(x+1)^2 - 4$ M1

$(0,-1)$

$-1 = k(1)^2 - 4$

$\Rightarrow k = 3$ A1

$y = 3(x+1)^2 - 4$

$y = 3(x^2 + 2x + 1) - 4$

$y = 3x^2 + 6x - 1$ A1

[9]

B4 Simultaneous Equations

1. $3x + 3y = -4$ $\quad 6x + 6y = -8$

$5x - 2y = 5$ $\quad 15x - 6y = 15$ added M1

$21x = 7$

$x = 1/3$ A1 $\quad 3(1/3) + 3y = -4$

$3y = -5$

$x = 1/3, y = -5/3$ A1

2. $y = x - 6$

$\frac{1}{2}x - y = 4$

$\frac{1}{2}x - (x - 6) = 4$ M1

$\frac{1}{2}x - x + 6 = 4$

$-\frac{1}{2}x = -2$

$x = 4$ A1 $\quad y = 4 - 6$

$y = -2$

$x = 4, y = -2$ A1

3. $3x^2 - x - y^2 = 0$ $\quad x + y = 1$

$y = 1 - x$

$3x^2 - x - (1-x)^2 = 0$ M1

$3x^2 - x - (1 - 2x + x^2) = 0$

$3x^2 - x - 1 + 2x - x^2 = 0$

$2x^2 + x - 1 = 0$ A1

$(2x - 1)(x + 1) = 0$

$x = 1/2$ $\quad x = -1$ A1

$y = 1 - 1/2$ $\quad y = 1 - -1$

$x = 1/2$ $y = 1/2$ A1 $\quad x = -1$, $y = 2$ A1

11

B5 Inequalities

1. $3(1 - 2t) \leq t - 4$

$3 - 6t \leq t - 4$

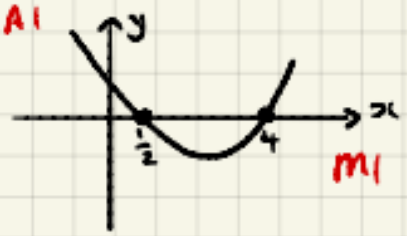
$7 \leq 7t$ M1

$t \geq 1$ A1

2. $2x^2 - 9x + 4 \leq 0$

$(2x - 1)(x - 4) \leq 0$ M1

CVs $x = 1/2$ $\quad x = 4$ A1



M1

$\frac{1}{2} \leq x \leq 4$ A1

3. $2y + 3 < 3y(y - 2)$

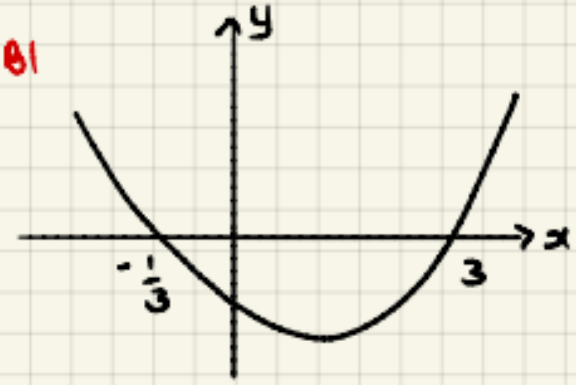
$2y + 3 < 3y^2 - 6y$

$0 < 3y^2 - 8y - 3$ B1

$3y^2 - 8y - 3 > 0$

$(3y + 1)(y - 3) > 0$ M1

CVs $y = -1/3$ $\quad y = 3$ A1



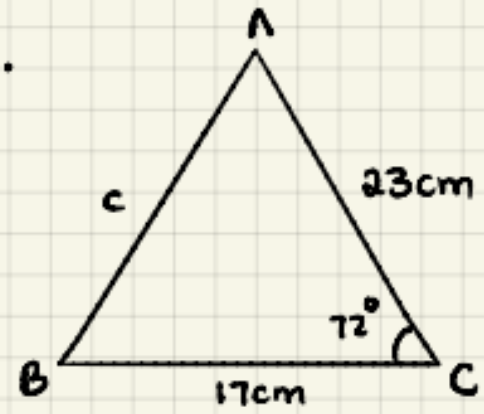
11

M1

$y < -1/3$ or $y > 3$ A1

E1 Triangle Geometry

1.



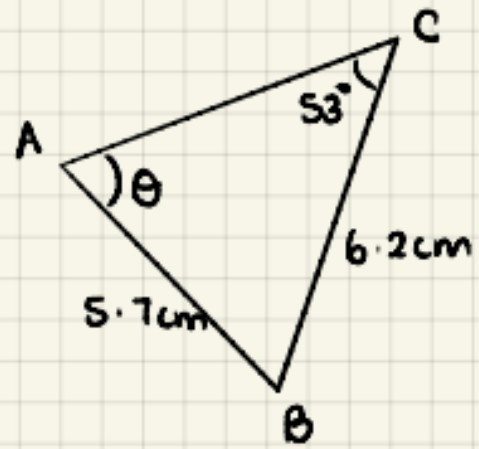
$c^2 = a^2 + b^2 - 2ab\cos C$

$c^2 = 17^2 + 23^2 - 2(17)(23)\cos 72^\circ$

$c^2 = 576.35$ M1

$AB = 24.0\text{cm}$ A1

2.

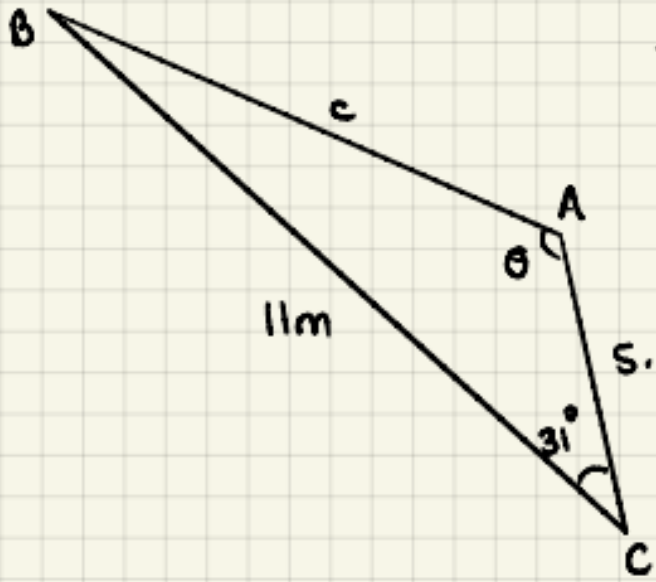


$\frac{\sin\theta}{6.2} = \frac{\sin 53}{5.7}$ M1

$\theta = \sin^{-1}\left(\frac{6.2\sin 53}{5.7}\right)$

$\theta = 60.3^\circ$ A1

3.



AB

$c^2 = 5.8^2 + 11^2 - 2(5.8)(11)\cos 31$

$c^2 = 45.27$ M1

$AB = 6.7\text{m}$ A1

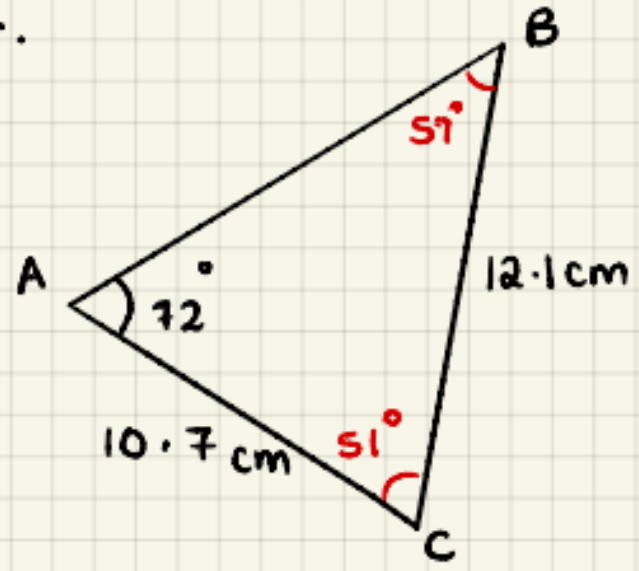
θ

$\cos\theta = \frac{5.8^2 + 6.7^2 - 11^2}{2(5.8)(6.7)}$ M1

$\theta = \cos^{-1}(-0.546)$ A1

$\theta = 123^\circ$

4.



$$\frac{\sin B}{10.7} = \frac{\sin 72^\circ}{12.1}$$ M1

$$B = \sin^{-1}\left(\frac{10.7 \sin 72^\circ}{12.1}\right)$$

$$\theta = 57^\circ$$ A1

$$A = \frac{1}{2} ab \sin C$$

$$= \frac{1}{2}(10.7)(12.1) \sin 51^\circ$$ M1

$$= 50.3 cm^2$$ A1

12

Year 12 Initial Test for Mathematics

Write out the solutions to each of the following questions.
*Show full working, **without** the use of a calculator.*

Practice 2 (No Calculator)

B1 Indices

1.	Evaluate $\left(3\frac{3}{8}\right)^{-1/3}$	**2.**	Express in the form x^k $\frac{\sqrt{x}\times\sqrt[5]{x}}{x^2}$	**3.**	Solve $3^{3x-2}=\sqrt[3]{9}$	**4.**	Solve $\left(\frac{1}{2}\right)^{1-x}=\left(\frac{1}{8}\right)^{2x}$

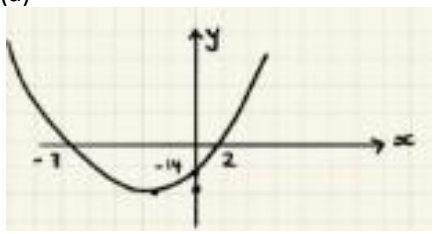
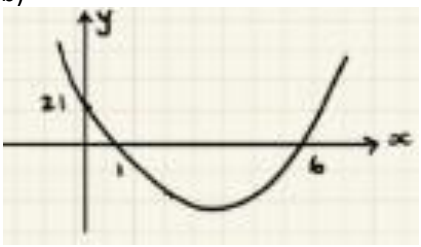
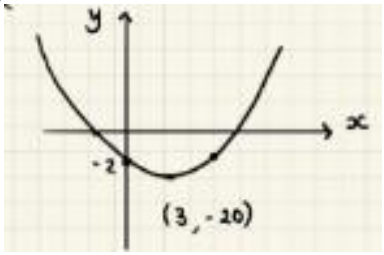
B2 Surds

1.	Simplify $\sqrt{80}$	**2.**	Expand and simplify $(7-3\sqrt{5})(3\sqrt{5}-2)$	**3.**	Rationalise the denominator $\frac{7}{5\sqrt{3}}$	**4.**	Rationalise the denominator $\frac{3+5\sqrt{11}}{7-\sqrt{11}}$

B3 Quadratics

1. Solve the following quadratic equations by factorising and use your solutions to sketch the related quadratic graph, labelling all intersections with the coordinate axis.		
(a) (i) $x^2-13x+40=0$	(b) (i) $x^2+5x=0$	(c) (i) $6x^2+5x-4=0$
(a) (ii) Sketch $y=x^2-13x+40$	(b) (ii) Sketch $y=x^2+5x$	(c) (ii) Sketch $y=6x^2+5x-4$

2. Solve the following quadratic equations by completing the square and use your solutions to sketch therelated quadratic graph, labelling all intersections with the coordinate axis and turning point.		
(a) (i) $x^2+2x-20=0$	(b) (i) $-11+8x-x^2=0$	(c) (i) $3x^2-18x+2=0$
(ii) Write $y=x^2+2x-20$ in the form $y=a(x+b)^2+c$	(ii) Write $y=-11+8x-x^2$in the form $y=a(x+b)^2+c$	(ii) Write $y=3x^2-18x+2$ in the form $y=a(x+b)^2+c$
(iii) Sketch $y=x^2+2x-20$	(iii) Sketch $y=-11+8x-x^2$	(iii) Sketch $y=3x^2-18x+2$

3. Evaluate the equation of the following quadratics, giving your answer in the form $y=ax^2+bx+c$		
(a) 	(b) 	(c) 

B4 Simultaneous Equations

1.	Solve $3x - 4y = 16$ $2x + 12y = 7$	**2.**	Solve $3y = 2x - 8$ $4x + y = -5$	**3.**	Solve $3x^2 - xy + y^2 = 36$ $x - 2y = 10$

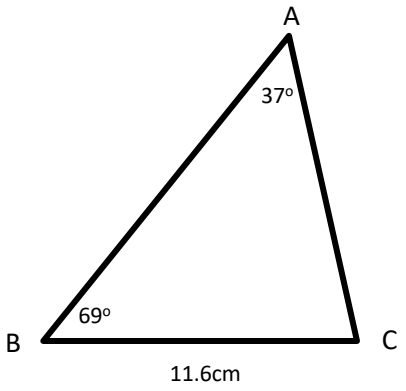
B5 Inequalities

Find the set of values for which…

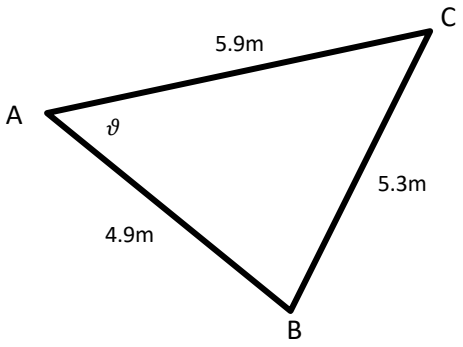
1.	$4(5 - 2y) \geq 3(7 - 2y)$	**2.**	$2x^2 - 5x - 3 > 0$	**3.**	$x(2x + 1) \leq x^2 + 6$

E1 Triangle Geometry (Calculator)

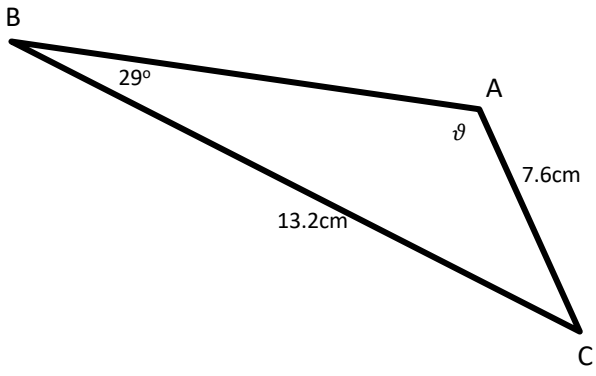
1. Calculate the length AB



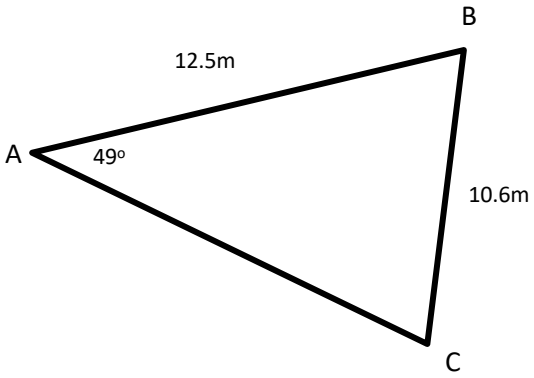
2. Calculate the angle ϑ



3. Calculate the length AB and the obtuse angle ϑ



4. Calculate the area of the triangle ABC



Practice Test 2

B1 Indices

1. $\left(3\frac{3}{8}\right)^{-1/3} = \left(\frac{27}{8}\right)^{-\frac{1}{3}}$ M1

$= \left(\frac{8}{27}\right)^{1/3}$

$= \frac{2}{3}$ A1

2. $\frac{\sqrt{x} \times \sqrt[5]{x}}{x^2}$

$= \frac{x^{1/2} \times x^{1/5}}{x^2}$ M1

$= \frac{x^{7/10}}{x^2}$ A1 $= x^{-13/10}$ A1

3. $3^{3x-2} = \sqrt[3]{9}$

$3^{3x-2} = (3^2)^{1/3}$ M1

$3^{3x-2} = 3^{2/3}$

$3x - 2 = \frac{2}{3}$ M1

$3x = \frac{8}{3} \Rightarrow x = \frac{8}{9}$ A1

4. $\left(\frac{1}{2}\right)^{1-x} = \left(\frac{1}{8}\right)^{2x}$

$(2^{-1})^{1-x} = (2^{-3})^{2x}$ M1

$2^{-1+x} = 2^{-6x}$

$-1 + x = -6x$ M1

$7x = 1$

$x = 1/7$ A1

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B2 Surds

1. $\sqrt{80}$

$= \sqrt{16 \times 5}$

$= 4\sqrt{5}$ A1

2. $(7 - 3\sqrt{5})(3\sqrt{5} - 2)$

$= 21\sqrt{5} - 14 - 45 + 6\sqrt{5}$ M1 A1

$= 27\sqrt{5} - 59$ A1

3. $\frac{7}{5\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$ M1

$= \frac{7\sqrt{3}}{15}$ A1

4. $\frac{3 + 5\sqrt{11}}{7 - \sqrt{11}} \quad \frac{(7 + \sqrt{11})}{(7 + \sqrt{11})}$ M1

$= \frac{21 + 8\sqrt{11} + 35\sqrt{11} + 55}{49 - 11}$ A1 A1

$= \frac{76 + 38\sqrt{11}}{38}$

$= 2 + \sqrt{11}$ A1

10

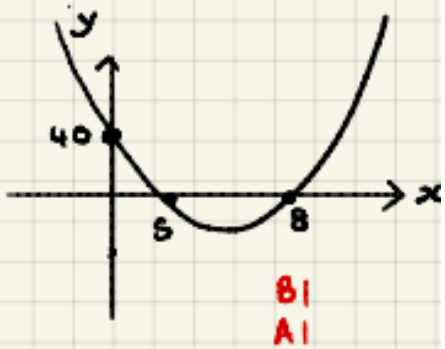
B3 Quadratics

1. (a) (i) $x^2 - 13x + 40 = 0$

$(x-8)(x-5) = 0$ M1

$x = 8 \quad x = 5$ A1

(ii) $y = x^2 - 13x + 40$



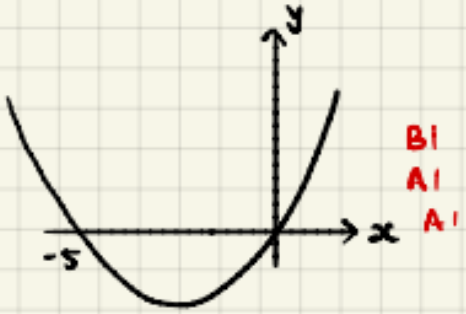
B1
A1
A1

(b) (i) $x^2 + 5x = 0$

$x(x+5) = 0$ M1

$x = 0 \quad x = -5$ A1

(ii) $y = x^2 + 5x$



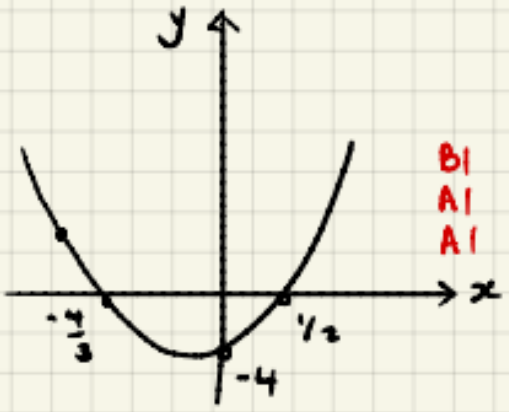
B1
A1
A1

(c) (i) $6x^2 + 5x - 4 = 0$

$(3x+4)(2x-1) = 0$ M1

$x = -4/3 \quad x = 1/2$ A1

(ii) $y =$



B1
A1
A1

15

B1 shape, location related to axes

A1 intersections x-axis

A1 intersections y-axis

2. (a) (i) $x^2 + 2x - 20 = 0$

$(x+1)^2 - 1 - 20 = 0$ M1

$(x+1)^2 = 21$

$x+1 = \pm\sqrt{21}$

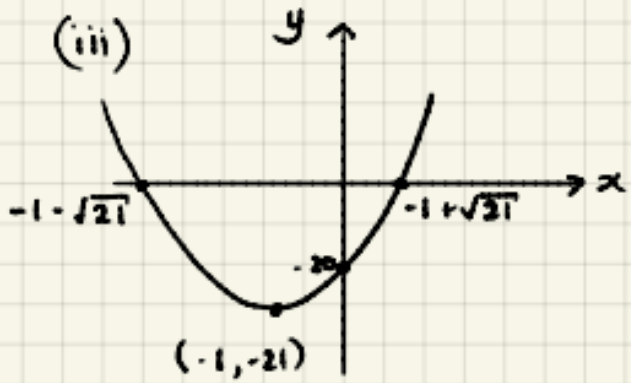
$x = -1 \pm \sqrt{21}$ A1

Graphs
- B1 Shape
- A1 Vertex
- A1 intersections x-axis
- A1 intersections y-axis

(ii) $y = x^2 + 2x - 20$

$y = (x+1)^2 - 21$ B1

(iii)



(b) (i) $-11 + 8x - x^2 = 0$

$-(x^2 - 8x + 11) = 0$ M1

$-[(x-4)^2 - 16 + 11] = 0$ M1

$5 - (x-4)^2 = 0$

$(x-4)^2 = 5$

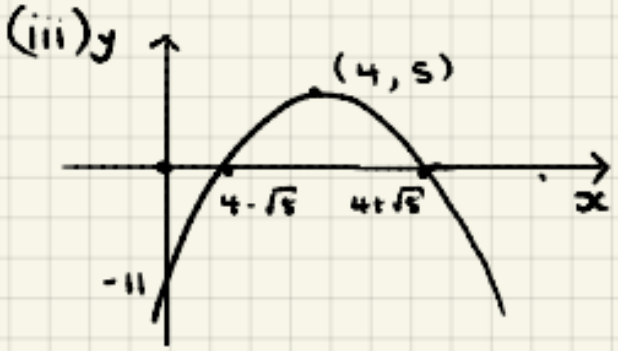
$x - 4 = \pm\sqrt{5}$

$x = 4 \pm \sqrt{5}$ A1

(ii) $y = -11 + 8x - x^2$

$y = 5 - (x-4)^2$ B1

(iii)



(c) (i) $3x^2 - 18x + 2 = 0$

$3\left[x^2 - 6x + \frac{2}{3}\right] = 0$ M1

$3\left[(x-3)^2 - 9 + \frac{2}{3}\right] = 0$ M1

$3\left[(x-3)^2 - \frac{25}{3}\right] = 0$

$3(x-3)^2 - 25 = 0$

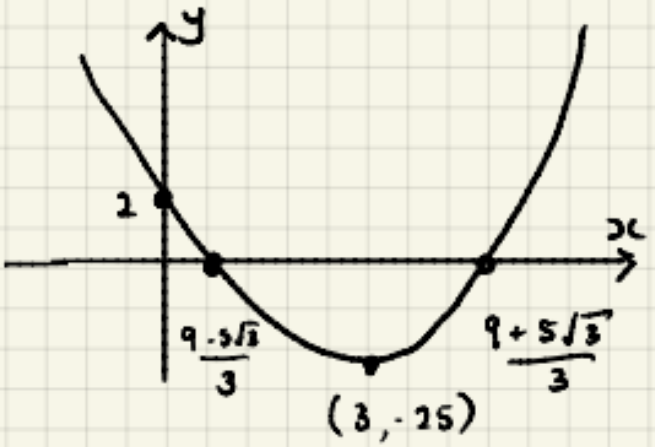
$3(x-3)^2 = 25$

$x - 3 = \pm\frac{5}{\sqrt{3}}$

$x = \frac{9 \pm 5\sqrt{3}}{3}$ A1

(ii) $y = 3x^2 - 18x + 2$

$y = 3(x-3)^2 - 25$ B1



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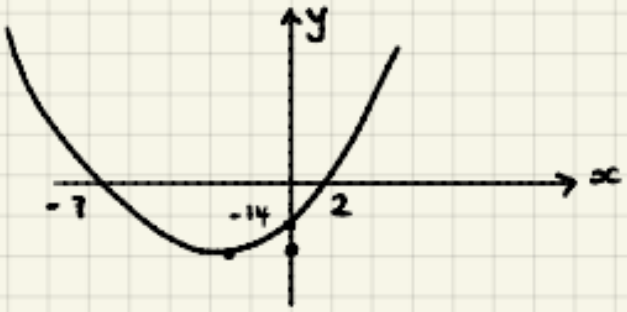
3. (a)



$y = k(x+7)(x-2)$ M1

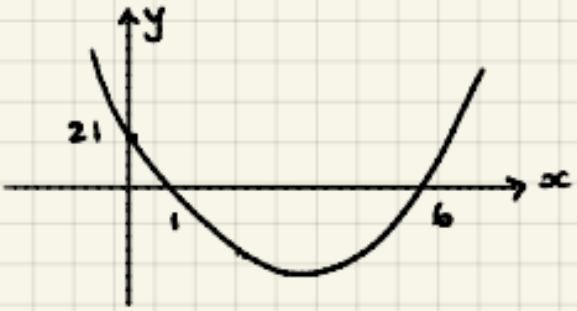
$-14 = k(7)(-2)$

$k = 1$ A1

$y = (x+7)(x-2)$

$y = x^2 + 5x - 14$ A1

(b)



$y = k(x-1)(x-6)$ M1

$21 = k(-1)(-6)$

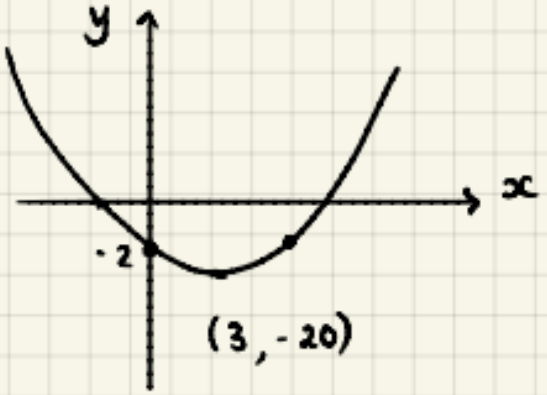
$\Rightarrow k = \frac{21}{6} = \frac{7}{2}$ A1

$y = \frac{7}{2}(x-1)(x-6)$

$y = \frac{7}{2}(x^2 - 7x + 6)$

$y = \frac{7x^2}{2} - \frac{49x}{2} + 21$ A1

(c)



$y = k(x-3)^2 - 20$ M1

$-2 = k(-3)^2 - 20$

$18 = k(9)$

$k = 2$ A1

$y = 2(x-3)^2 - 20$

$y = 2(x^2 - 6x + 9) - 20$

$y = 2x^2 - 12x - 2$ A1

9

B4. Simultaneous equations

1. $3x - 4y = 16$ $\quad 9x - 12y = 48$

$2x + 12y = 7$ $\quad 2x + 12y = 7$ M1

$11x = 55$

$x = 5$ A1

$3x - 4y = 16$

$15 - 4y = 16$

$-1 = 4y$

$y = -1/4$

$x = 5, y = -1/4$ A1

2. $3y = 2x - 8 \Rightarrow 2x = 3y + 8$

$4x + y = -5$ $\quad 4x = 6y + 16$ M1

$6y + 16 + y = -5$

$7y = -21$

$y = -3$

$2x = 3y + 8$

$2x = 3(-3) + 8$

$x = -1/2$ A1 $\quad x = -1/2$ $y = -3$ A1

3. $3x^2 - xy + y^2 = 36$

$x - 2y = 10 \Rightarrow x = 2y + 10$

$3(2y+10)^2 - (2y+10)y + y^2 = 36$ M1

$3(4y^2 + 40y + 100) - y(2y+10) + y^2 = 36$

$12y^2 + 120y + 300 - 2y^2 - 10y + y^2 = 36$

$11y^2 + 110y + 264 = 0$

$y^2 + 10y + 24 = 0$ A1

$(y+6)(y+4) = 0$

M1

$y = -6$ $\quad y = -4$

$x = 2(-6) + 10$ $\quad x = 2(-4) + 10$

$x = -2$ $\quad x = 2$

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$x = -2$, $y = -6$ A1 $\quad x = 2$, $y = -4$ A1

BS Inequalities

1. $4(5-2y) \geqslant 3(7-2y)$

$20 - 8y \geqslant 21 - 6y$ M1

$-1 \geqslant 2y$

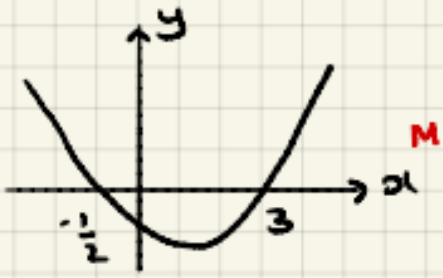
$-\frac{1}{2} \geqslant y$

$y \leqslant -\frac{1}{2}$ A1

2. $2x^2 - 5x - 3 > 0$

$(2x+1)(x-3) > 0$ M1

CVs $x = -\frac{1}{2}$ $x = 3$ A1



M1

$x < -\frac{1}{2}$ or $x > 3$ A1

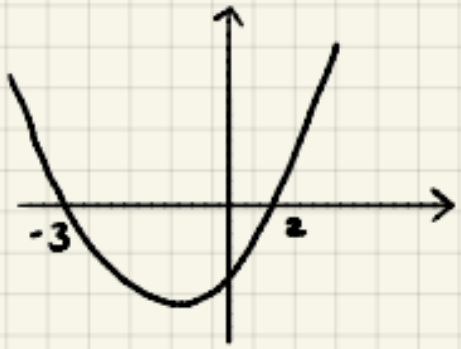
3. $x(2x+1) \leqslant x^2 + 6$

$2x^2 + x \leqslant x^2 + 6$ M1

$x^2 + x - 6 \leqslant 0$

$(x+3)(x-2) \leqslant 0$ M1

CVs $x = -3$ $x = 2$ A1



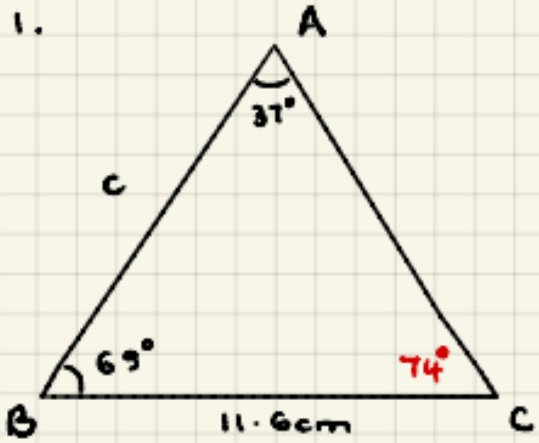
M1

$-3 \leqslant x \leqslant 2$ A1

11

E1 Triangle Geometry

1.

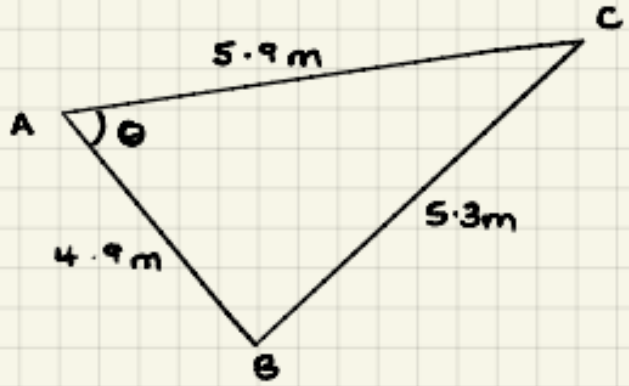


$$\frac{c}{\sin 74^\circ} = \frac{11.6}{\sin 37^\circ}$$

$$c = \frac{11.6 \sin 74^\circ}{\sin 37^\circ} \quad \text{M1}$$

$$c = 18.5\text{cm} \quad \text{A1}$$

2.



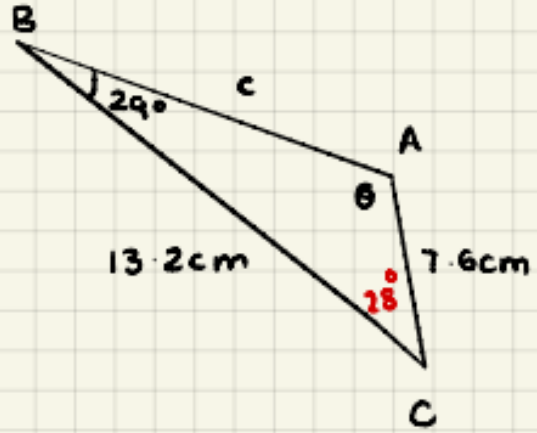
$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos\theta = \frac{5.9^2 + 4.9^2 - 5.3^2}{2(5.9)(4.9)} \quad \text{M1}$$

$$\cos\theta = 0.53148$$

$$\theta = 57.9^\circ \quad \text{A1}$$

3.



θ

$$\frac{\sin\theta}{13.2} = \frac{\sin 29}{7.6}$$

$$\sin\theta = \frac{13.2 \sin 29^\circ}{7.6} \quad \text{M1}$$

$$\sin\theta = 0.8420$$

$$\theta = 57.4^\circ$$

obtuse $\Rightarrow \theta = 123^\circ$ A1

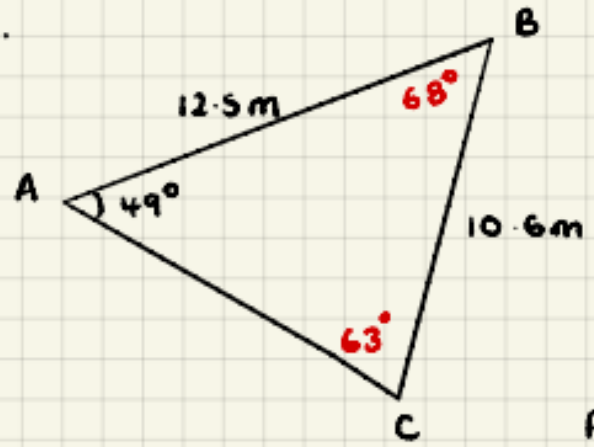
AB

$$c^2 = a^2 + b^2 - 2ab\cos C$$

$$c^2 = 13.2^2 + 7.6^2 - 2(13.2)(7.6)\cos 28 \quad \text{M1}$$

$$c^2 = 54.8 \Rightarrow c = 7.4\text{cm} \quad \text{A1}$$

4.



$$\frac{\sin C}{12\cdot5} = \frac{\sin 49^\circ}{10\cdot6}$$

$$\sin C = \frac{12\cdot5 \sin 49}{10\cdot6} \quad M1$$

$$C = 63^\circ \quad A1$$

Area $= \frac{1}{2}\, ab \sin C$

Area $= \frac{1}{2}\,(12\cdot5)(10\cdot6)\sin 68^\circ$ M1

Area $= 61\cdot5\ m^2$ A1

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